

# Lateral variations of $P_n$ velocity and anisotropy in Taiwan from travel-time tomography

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In this study, the  $P$  arrivals of 1726 ray paths with the epicentral distances longer than 200 km from 539 earthquakes that occurred in Taiwan are used to investigate the variation of  $P_n$  velocity. The results show that the lateral variation of  $P_n$  velocity in Taiwan is quite similar to the pattern of gravity anomaly and strongly related to several features of Taiwan's geological structure. The crust is a little thicker (about 39 km) in the Central Range and somewhat thinner toward the east and west. A relatively thin crust (about 35 km) is obtained in the area of Peikang High; however, an unexpected thick crust of greater than 40 km is also found at the corner of southwestern Taiwan. The degree of anisotropy of  $P_n$  velocity is found less than 10% and the fast direction is generally in the E-W direction. This direction is parallel to the axis of compressional stress or the direction of plate motion, indicating that the anisotropy results from the deformation of the upper mantle.

**Key words:**  $P_n$ , anisotropy, tomography.

## 1. Introduction

Taiwan is located at the boundary between the Philippine Sea and Eurasian plates, and one of the most spectacular arc-continent collisions occurs there. A better understanding of the subterranean structure of this area is an important topic for geological and geophysical scientists; however, from the past studies, there is little agreement on the dynamic processes responsible for the crust-mantle structure of the island and surrounding areas (Suppe, 1981, 1985; Rau and Wu, 1995). Lateral variation of  $P_n$  velocity is associated with the changes of the temperature, pressure, and material in upper mantle, while variation in crustal thickness has resulted from many different factors including crustal extension or compression, isostatic forces, and magma intrusion (Black and Braile, 1982). Thus, knowledge about the crustal thickness and  $P_n$  velocity can provide valuable information on crustal deformation, and help us to infer the tectonic evolution of the study area.

In Taiwan, an average of  $P_n$  velocity with 7.8 km/s was first given by Yeh and Tsai (1981). Later, Huang *et al.* (1998) presented the regionalized  $P_n$  velocities with 8.2 km/s, 7.9 km/s, and 8.0 km/s for the regions of the Taiwan Strait, Taiwan Island, and Eastern Coastal Range, respectively. Lateral variations of the crustal thickness and upper mantle  $P$ -wave velocity were estimated by several studies from 3-D velocity inversion (Chen *et al.*, 1994; Rau and Wu, 1995; Ma *et al.*, 1996).

The anisotropic properties in the upper mantle are considered to be related to the shear stress of plate motion (Raitt *et al.*, 1969; Okal and Talandier, 1980; Hearn, 1984). Kuo *et*

*al.* (1994) have observed a certain degree of anisotropy for  $P_n$  velocity in upper mantle of the northern Taiwan. In our current study, the travel times of  $P_n$  are used to derive better images of the lateral variations of the  $P_n$  velocity and its anisotropy. Meanwhile, the corresponding crustal thickness is also estimated. From these results, a better explanation of the tectonic evolution in Taiwan area is inferred.

## 2. Tectonic Setting

The geological structures of Taiwan trend mainly in a NNE-SSW direction as shown in the simplified geological map (Fig. 1). These trends are parallel to the main topographic trends. The topography of Taiwan is dominated by the Central Range where pre-Tertiary metamorphic complexes are exposed. They are most probably exhumed lower crustal material raised to the upper level as a result of recent orogeny (Ho, 1986; Lin, 2000). East of the metamorphic complex is the Coastal Range. These layers are thrust up along a series of echelon faults, striking about N30°E, with a small angle to the dominant structural trend of the island. These thrust layers were successively accreted to the island, beginning around 4–6 million years before present (Lee *et al.*, 1991). The Longitudinal Valley separates the Coastal Range from the Central Range to the west, and is considered to be the suture that juxtaposes older continental rocks and young island arc materials. It also separates the highly seismic Coastal Range (Wu *et al.*, 1989) from the relatively aseismic Central Range. To the west of the pre-Tertiary metamorphic complex are the main Central Range, the Foothills and the Coastal Plain. The Peikang high, as a pre-Tertiary basement, separates the western Taiwan into two parts: the pro-orogenic sedimentary material in north-western Taiwan were formed in relatively shallow shelf envi-

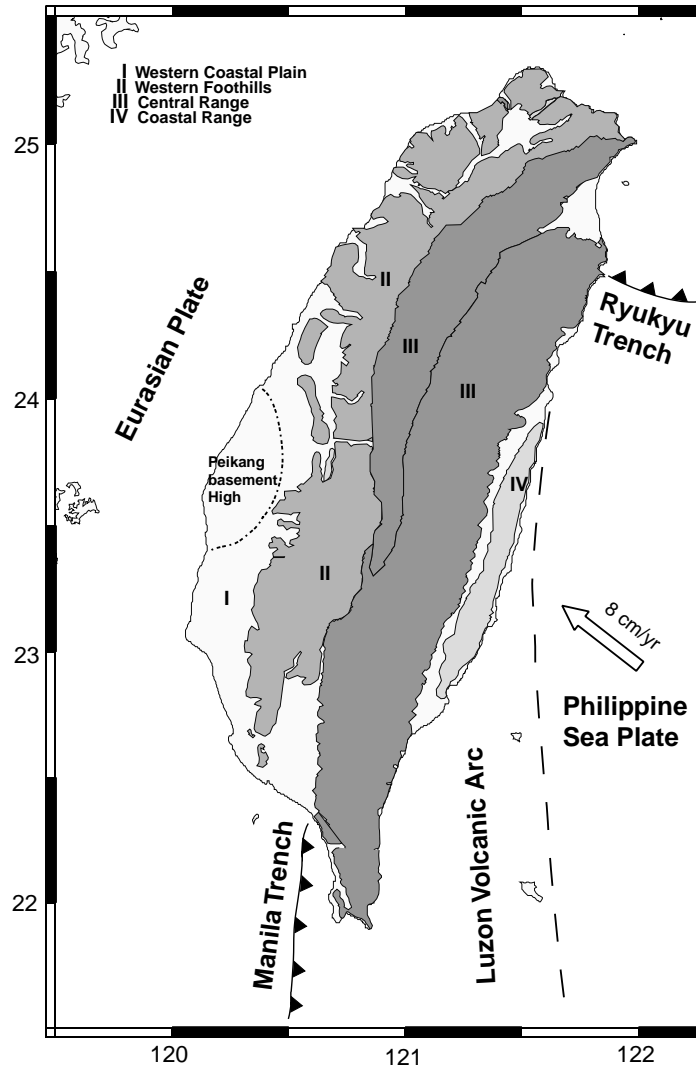


Fig. 1. A simplified structural geology map of Taiwan showing: (a) The regional tectonic stress due to the convergence of the Philippine Sea and the Eurasia Plates. (b) The major geological regimes in Taiwan: I. Western Coastal Plain, II. Western Foothills, III. Central Range (forms the backbone of Taiwan), and IV. Coastal Range. The dashed region on the western coast shows the approximate location of the Peikang High (PKH), which is the Tertiary basement high detected from seismic reflection mapping.

ronments, whereas the material in the south-western Taiwan were formed along the former continental slope, as a part of the passive margin of southeastern China. The Coastal Plain of western Taiwan is composed of Quaternary alluvial deposits, at the shallow depths. The Neogene strata underneath the alluvial are gently folded and getting thinner to the west.

### 3. Data and Methodology

In this study, the  $P$ -arrivals of earthquakes in Taiwan area as recorded by the Central Weather Bureau Seismic Network (CWBSN) during the period between 1993 and 2001 have been used. To obtain a high quality data set and ensure that the  $P$ -arrivals were  $P_n$  phases, a few criteria for selecting the final data were followed: (a) the epicentral distance is greater than 200 km; (b) the focal depth is less than 25 km; (c) the errors of hypocenter determination are within 3 km in horizontal, and 5 km in vertical; (d) the  $P_n$  arrivals are picked with errors less than  $\pm 0.1$  s (i.e. the weightings assigned by CWB of observations belong to 0, 1, and 2 only). Based on these criteria, a total of 1768 ray paths from 539 events are

selected as the data set for  $P_n$  velocity inversion. The ray paths shown in Fig. 2 are quite well distributed in crossover the Taiwan area.

In order to investigate the lateral variation of  $P_n$  velocity, the area of Taiwan ( $21.6^\circ\text{N}$  to  $25.6^\circ\text{N}$ ,  $119.8^\circ\text{E}$  to  $122.2^\circ\text{E}$ ) is divided into 240 blocks, thus each block size is  $0.2^\circ \times 0.2^\circ$ . The total travel time of each path is the sum of the time across the blocks plus the time-term corrections for the station and source as shown in the following equation (Zhao and Xie, 1993):

$$t_{ij} \approx \frac{X_{ij}}{V_{ij}^0} = \sum \Delta_{ijk} S_k + a_i + b_j \quad (1)$$

where  $t_{ij}$  is the travel time of the path from event  $i$  to station  $j$ ;  $X_{ij}$  is the epicentral distance of the path;  $V_{ij}^0$  is the average  $P_n$  velocity of the path (Zhao and Xie, 1993);  $\Delta_{ijk}$  is the length of the ray path in block  $k$ ;  $S_k$  is the slowness of block  $k$ ;  $a_i$  and  $b_j$  are the time-term corrections for station and source. If the azimuthal anisotropy is taken into account,

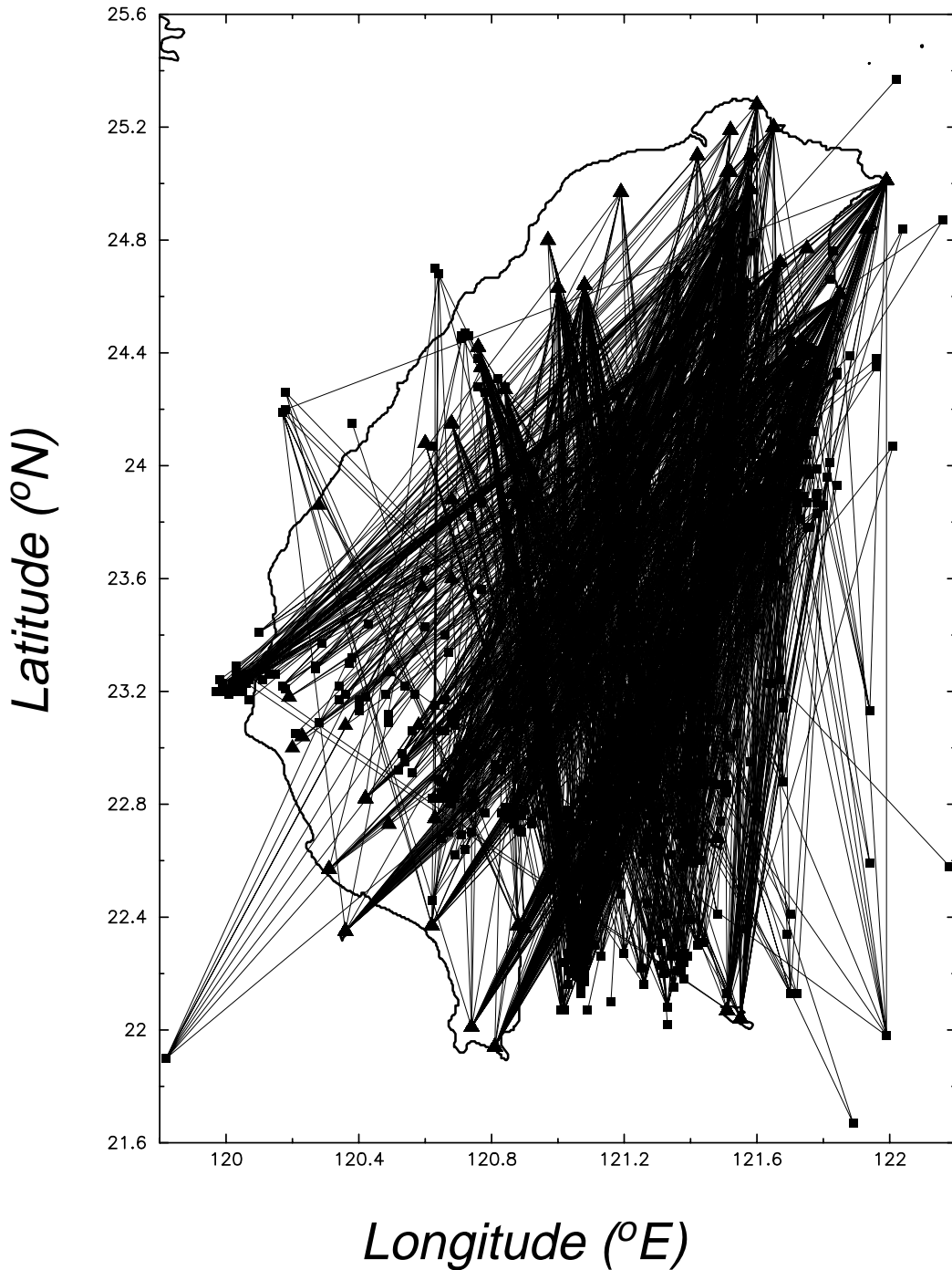


Fig. 2. Ray paths. Solid triangle and square represent the locations of seismic stations and epicenters, respectively.

then the equation becomes (Hearn, 1996)

$$\frac{1}{V_{ij}^o} = \frac{1}{X_{ij}} \sum (S_k + A_k \cos 2\phi + B_k \sin 2\phi) * \Delta_{ijk} + \text{Res}_{ij} \quad (2)$$

where,  $A_k$  and  $B_k$  are the anisotropic coefficients and  $\phi$  is the angle of fast direction as measured from the north. The quantity  $(A_k^2 + B_k^2)^{1/2}$  represents the magnitude of anisotropy and  $\phi = \frac{1}{2} \tan^{-1}(B_k/A_k)$ .

After rearranging the Eq. (2) and simplifying, we obtain

$$\frac{1}{V_{ij}^o} = \frac{\sum \Delta_{ijk}(S_k + A_k \cos 2\phi + B \sin 2\phi)}{X_{ij}} + R_{ij} \quad (3)$$

where

$$R_{ij} \approx \frac{\delta a_i + \delta b_j}{X_{ij}} \quad (4)$$

is the error between theoretical calculations and observations. Solving Eq. (3) by the back-projection method (Xie and Mitchell, 1990), the values of  $P_n$  velocity and the coefficients of anisotropic terms are obtained. The resolution of the inversion results is expressed as the Point Spread Function (PSF) (Zhao and Xie, 1993). Assuming that the travel-time residual of the  $P_n$  velocity inversion predominantly results from the lateral variation of the Moho depth (Zhao and Xie, 1993; Baumont *et al.*, 2001), we can solve for  $\delta a_i$  and

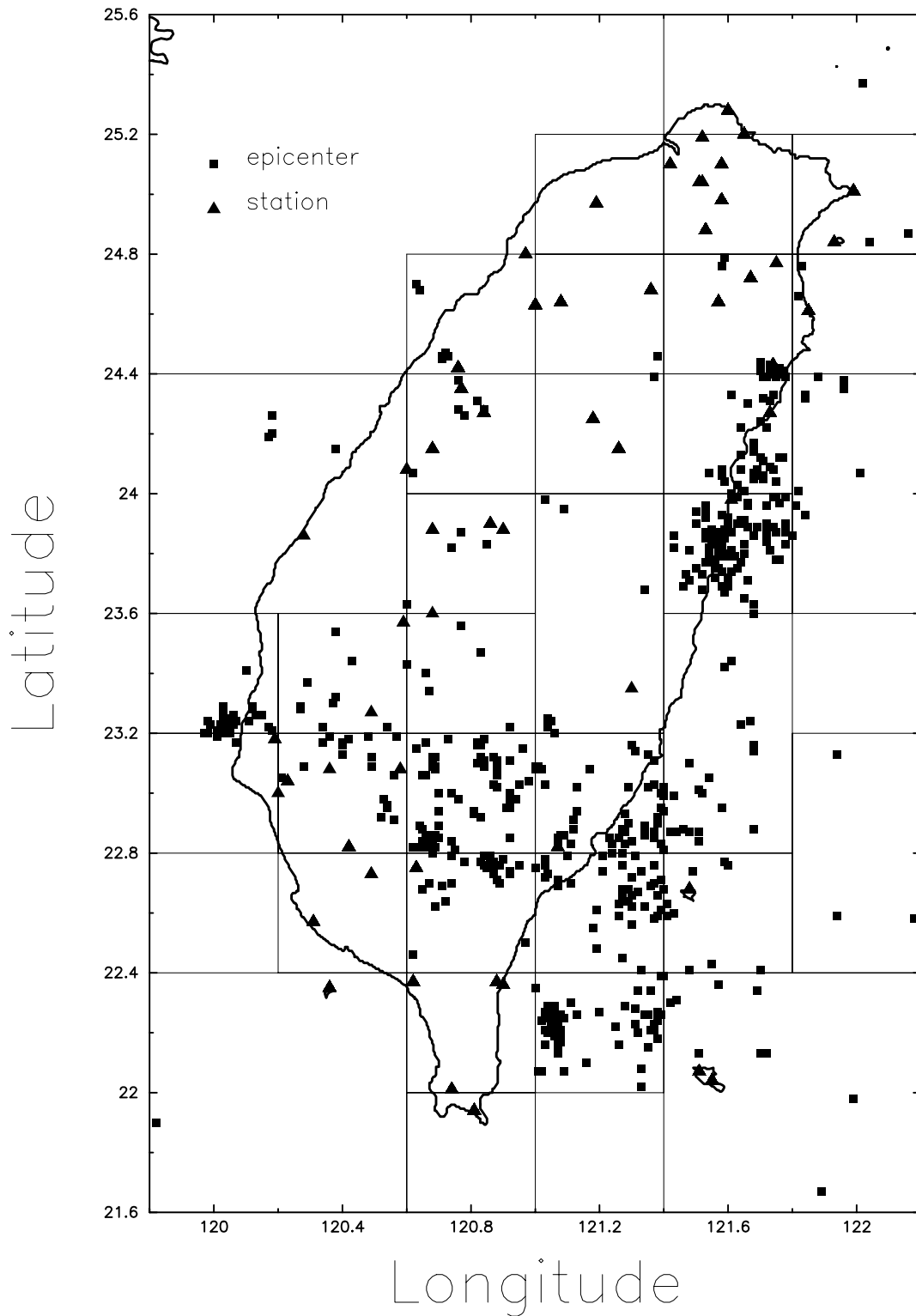


Fig. 3. Sub-regions used in the Moho depth inversion.

$\delta b_i$  with the known  $R_{ij}$ . With the improvements in estimation Moho depth, we recalculate the  $P_n$  velocities. Through an iteration procedure we are able to obtain  $P_n$  velocity and Moho depth with minimum travel-time residuals. For making this inversion overdetermined, and reducing errors in original times, in event locations and arrival-time readings, we merge the unknowns  $\delta a_i$  and  $\delta b_i$  into a new set of unknowns (Zhao and Xie, 1993) according to the distributions

of stations and epicenters (Fig. 3), and the Moho depth in the subregion is assumed constant.

#### 4. Results and Discussion

Before inversion, the appropriate initial values of the crustal thickness ( $H$ ), the crustal  $P$  velocity ( $V_c$ ), and the upper mantle  $P$  velocity ( $V_m$ ) have to be estimated. In doing this, the regression method presented by Zhao and Xie

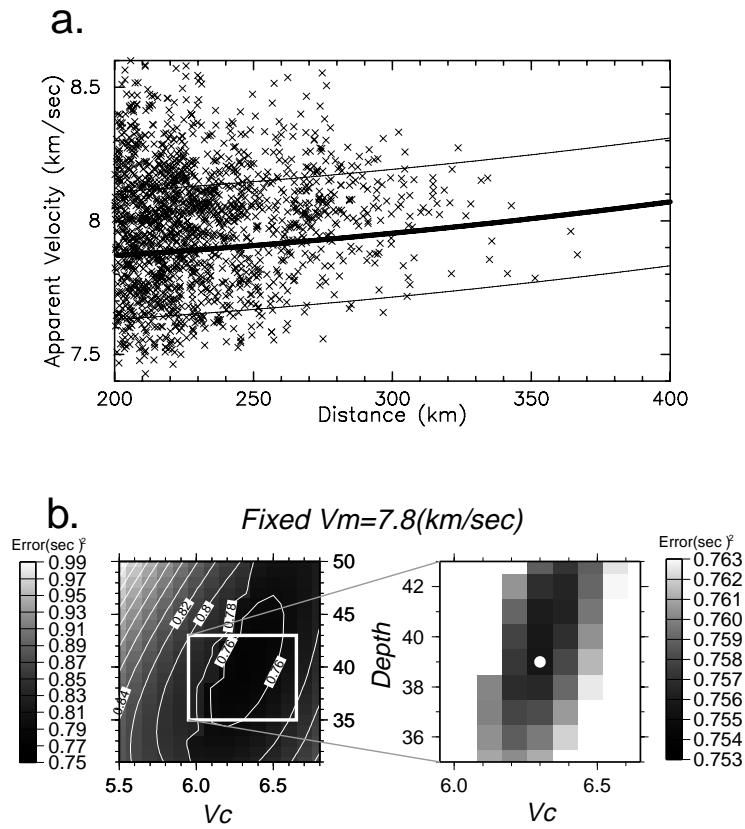


Fig. 4. (a)  $P_n$  travel time curve (bold line) derived from linear regression of arrival time data used in this study. Two thin lines represent the standard errors in fitting. A slight dependence of velocity on the travel distance indicates that the ray paths used in this study do not penetrate the deep mantle. (b) The distribution of RMS travel time residual for various combination of the average crustal  $P$  velocity ( $V_c$ ) and Moho depth with fixed mantle  $P$  velocity ( $V_m$ ).

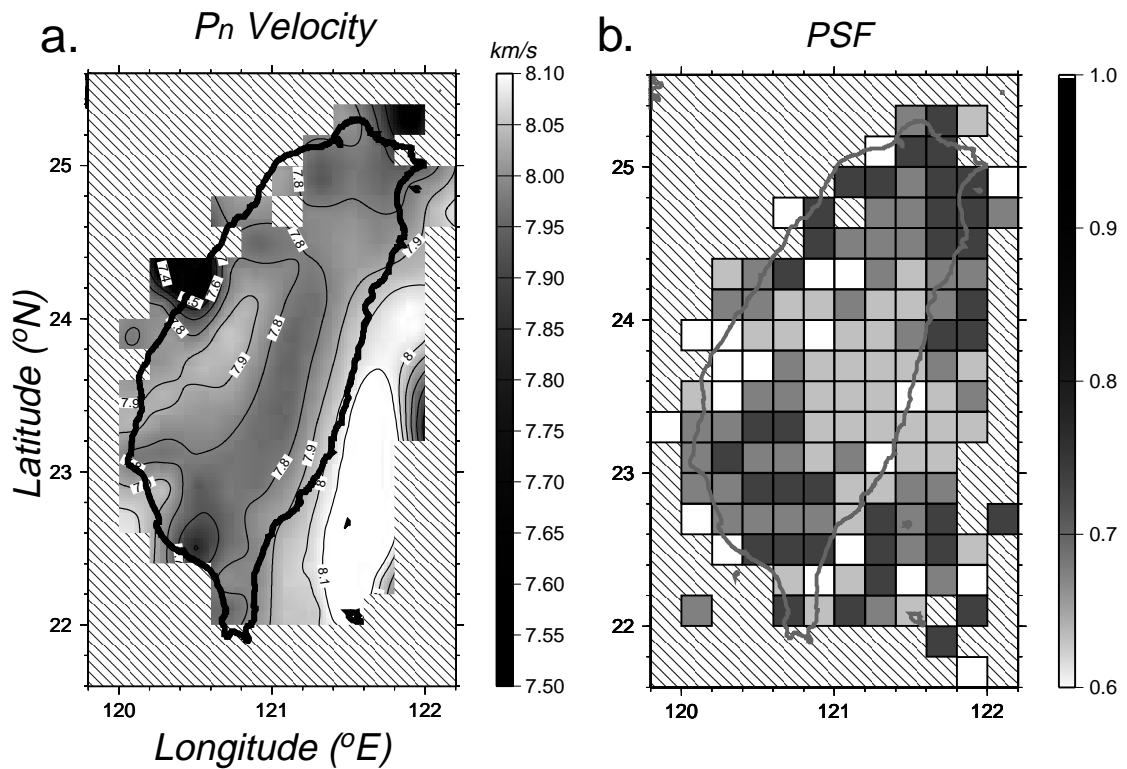


Fig. 5. (a) The  $P_n$  velocity distribution derived from travel time tomography. (b) The PSF distributions for model blocks. Note that the blocks with PSF values lower than 0.6 are represented by oblique line. It shows that the inversion can resolve the dimension roughly the same as that of the Taiwan Island.

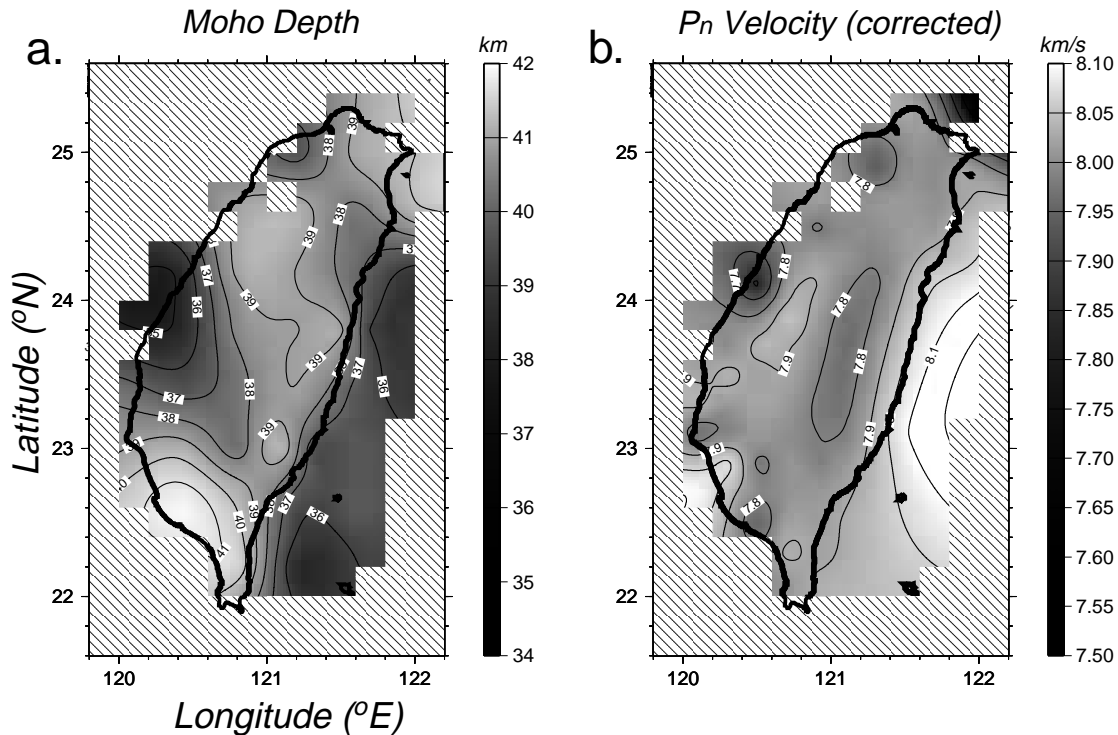


Fig. 6. (a) The Moho depth distribution. (b) The corrected  $P_n$  velocity distribution.

(1993) is applied to estimate the upper mantle  $P$  velocity ( $V_m$ ) (Fig. 4(a)); then, fixing  $V_m$ , and taking various combinations of  $H$  and  $V_c$ , the optimal values of  $H$  and  $V_c$  are obtained when the minimum travel-time residual of inversion is found (Fig. 4(b)). According to these procedures, the values of 7.8 km/s, 6.3 km/s, and 39 km for  $V_m$ ,  $V_c$ , and  $H$ , are obtained, respectively. These values are used as the initial values for inversion of Eq. (3). The lateral variation of  $P_n$  velocity, as shown in Fig. 5(a), is derived by the back-projection method. The spatial resolution at a given cell can be estimated by the point-spreading function (PSF) calculated for the cell (e.g. Humphreys and Clayton, 1988; Xie and Mitchell, 1990; Zhao and Xie, 1993). We calculated the PSF of each block and found that the spreading of PSF is generally within about  $0.3^\circ$  (three blocks). For a full understanding of the distribution of the degrees of resolutions of the blocks in the entire research area, Figure 5(b) shows the PSF values of each central block (which is similar to the diagonal element of the resolution matrix in the least square inversion). The path average travel-time residual after  $P_n$  velocity inversion is roughly 0.753 s as shown in Fig. 4(b). Using Eq. (4), the variation of crustal thickness in Taiwan is calculated and shown in Fig. 6(a). Based on this crustal thickness the lateral variation of  $P_n$  velocity is also corrected and shown in Figure 6(b). The path average travel-time residual (0.172 s) after Moho depth correction is 77% less than that before inversion. The distribution of corrected  $P_n$  velocity agrees well with the pattern of gravity anomaly given by Yen *et al.* (1998). A zone, covering most of the Central Range, is found to have a crustal thickness of about 39 km and  $P_n$  velocity of about 7.8 km/s, suggesting that the low velocity observation in the Central Range may not only reflect the high thermal gradient on, but also the variation in

crustal thickness. The crust becomes thinner in both western and eastern Taiwan as compared with the Central Range. The area of Peikang High, which played an important role in tectonic evolution of Taiwan during late Miocene, also has a relative thinner crust (about 35 km) compared to its surroundings. In eastern offshore region, the thinner crust represents the transition structure of the Philippine Sea Plate. A crustal thickness greater than 40 km at the corner of southwestern Taiwan has probably resulted from the spreading of the South China Sea in the past, and the Eurasian Plate was dragged down to the mantle (Chemenda *et al.*, 1995, 1996). The deeper Moho depth is also shown by wide-angle reflection profile analysis (Shih *et al.*, 2001).

Figure 7(a) shows the distribution of anisotropy for  $P_n$  velocity in Taiwan area. Figures 7(b) and 7(c) show the error distributions of the anisotropic coefficient components  $A_k$  and  $B_k$ . From Fig. 7(a), it is easily seen that the fast directions for  $P_n$  velocity are nearly in the E-W direction. The degree of anisotropy is less than 10%, and the anisotropy in western Taiwan is a little greater than that in eastern. Although a few inconsistent directions are found, but, in general, the fast direction is almost parallel to the axis of compressional stress or the direction of plate motion. This result is consistent with the result obtained from a study of shear wave splitting in western Taiwan (Chen and Yen, 1998). Similar results have also given by Hearn (1996) in California.

## 5. Conclusion

From a thorough study on the distributions of the crustal thickness,  $P_n$  velocity, and anisotropy in Taiwan area, a few conclusions are given below:

- (1) The variations of crustal thickness and  $P_n$  velocity

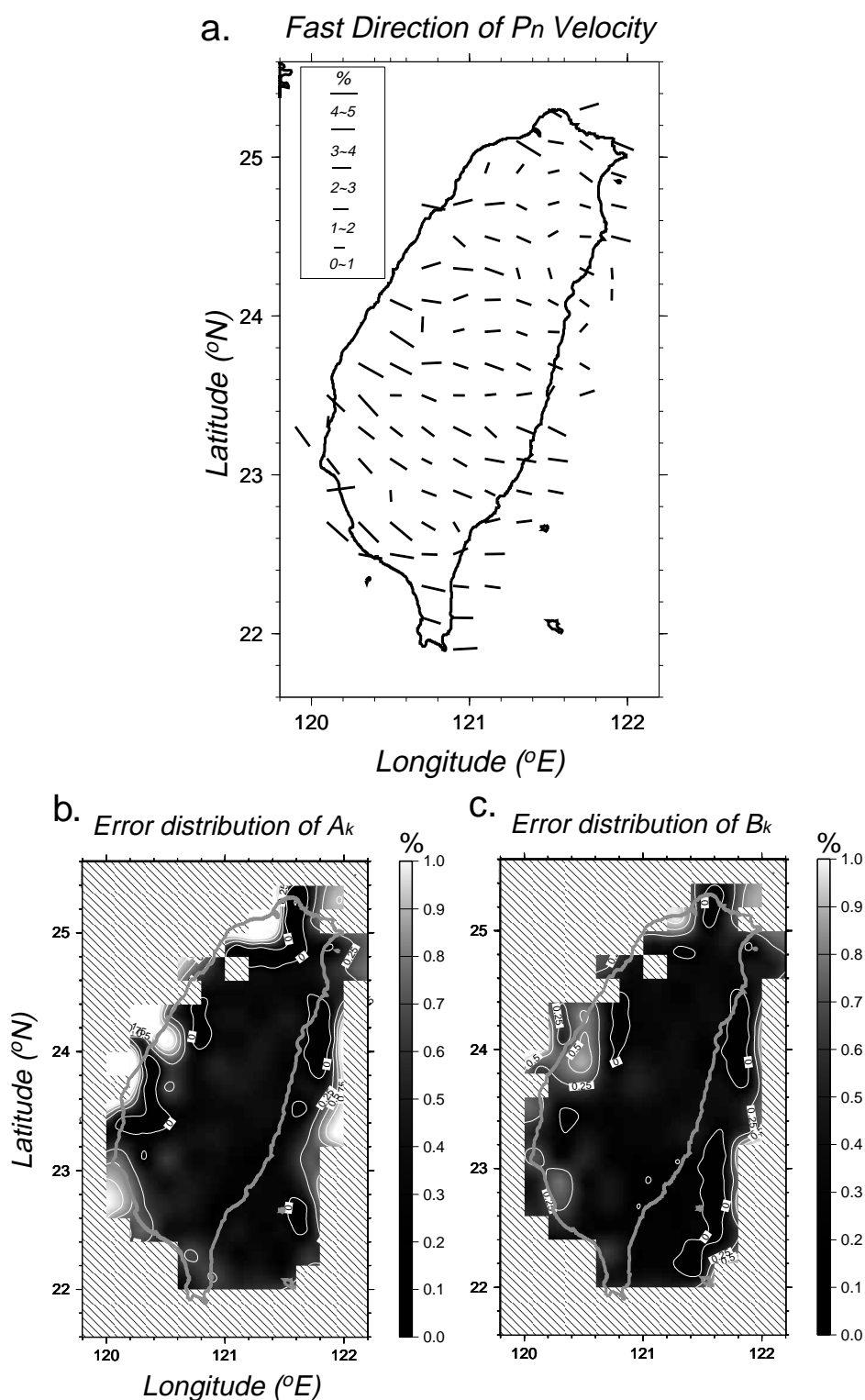


Fig. 7. (a) Distribution of the direction of fast  $P_n$  velocity. The length of solid line represents the magnitude of anisotropy. The errors of the anisotropic coefficients ( $A_k$  and  $B_k$ ) are also shown in (b) and (c).

are quite similar to the distribution of gravity anomaly and strongly related to the feature of geological structures in Taiwan.

(2) The area of Peikang High, an important geological structure in western Taiwan, has a relative thinner crust to its surroundings. An unexpected crustal thickness of greater than 40 km is also found at the corner of southwestern Tai-

wan.

(3) The degrees of anisotropy for  $P_n$  velocity are less than 10%, and the fast direction is nearly E-W in general. This direction is parallel to the axis of compressional stress or the direction of plate motion, indicating that the anisotropy results from the deformation of upper mantle beneath Taiwan area.

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